Fourth Semester B.E. Degree Examination, Aug./Sept.2020 Signals and Systems

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module. 2. Missing data, if any, may be suitably assumed.

Module-1

- a. Explain the following with an example each: 1
 - i) Even and odd signal
 - ii) Aperiodic and periodic signal
 - iii) Energy and power signal.

(06 Marks)

b. Sketch the following signal:

i)
$$y(t) = r(t+2) - r(t+1) - r(t-1) + r(t-2)$$

ii)
$$y(t) = r(t+2) - r(t+1) - r(t-1) + r(t-2)$$

(06 Marks)

Verify the following properties of system: memoryless, casual, stable and some invariant y(n) = n x(n).

(08 Marks)

Sketch the even and odd parts of the signal shown in the Fig.Q2(a

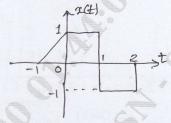


Fig.Q2(a)

(06 Marks)

- Classify the following the following as an energy or power signal
 - i) y(t) = r(t) r(t-2)

ii)
$$x(t) = (1 + e^{-5t})u(t)$$
.

(08 Marks)

c. Determine whether the following signals are periodic or not. If periodic find its fundamental time period.

i)
$$x[n] = 5\sin\left(\frac{7\pi n}{12}\right) + 8\cos\left(\frac{14\pi n}{8}\right)$$

ii)
$$x(t) = \cos t + \sin \sqrt{2}t$$
.

(06 Marks)

Module-2

- Prove the following properties of convolution:
 - i) Commutative ii) Distributive.

(06 Marks)

b. Determine the convolution of the following two signals $x(t) = e^{-3t}u(t)$ and h(t) = u(t+2).

(07 Marks)

Find the convolution of the following sequences

$$x(n) = \beta^n u(n)$$
 with $|\beta| < 1$ and $h(n) = u(n-3)$.

(07 Marks)

OR

4 a. Determine the convolution sum of the given sequence $x(n) = \{1, 2, 3, 1\}$ and $h(n) = \{1, 2, 1, -1\}$ sketch output.

(06 Marks)

b. The impulse response of the system is given by h(t) = u(t). Determine the output of the system for an input $x(t) = e^{-\alpha t} u(t)$.

(08 Marks)

c. Prove the associative property of convolution.

(06 Marks)

Module-3

5 a. Find the step response for the impulse response h(t) = u(t+1) - u(t-1). (06 Marks)

5. Find the overall impulse response of a cascade of two systems having identical impulse responses h(t) = 2[u(t) - u(t-1)]. (06 Marks)

c. Find the Fourier series coefficients X(k) for the signal $x(t) = \sum_{m=-\infty}^{\infty} [\delta(t - \frac{1}{2}m)]$. Sketch the magnitude and phase spectra. (08 Marks)

OR

6 a. Determine whether following system with the given impulse response is memoryless, causal and stable $h[n] = \left[\frac{1}{2}\right]^n u[n]$. (06 Marks)

b. Evaluate the DTFS representation for the signal x(n) shown in Fig.6(b) and sketch its spectra.

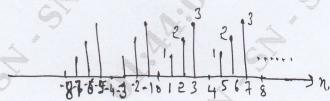


Fig.Q6(b)

(08 Marks)

c. Find the Fourier series representation for the signal $x(t) = \sin(2\pi t) + \cos(3\pi t)$. Sketch the magnitude and phase spectra. (06 Marks)

Module-4

7 a. Prove the following properties of Fourier transform:

i) Time shifting

ii) Time domain convolution.

(08 Marks)

b. Find the Fourier transform of the signal.

(06 Marks)

c. Find the DTFT of the signal shown in the Fig.Q7(c).

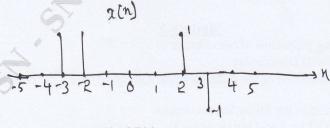


Fig.Q7(c) 2 of 3

(06 Marks)

OR

8 a. Explain the concept of sampling theorem and reconstruction of signals.
b. Find the DTFT of the sequence x(n) = -aⁿ u[-n-1].
c. Find the Fourier transform of the signal x(t) = e^{-3t} u(t-1).
(06 Marks)
(06 Marks)

Module-5

- a. Explain the properties of ROC.
 b. Find the Z-transform and the ROC of the discrete sinusoid signal.
 x[n] = [sin(Ωn)]u[n].
 (07 Marks)
 - c. Find the transfer function and difference equation if the impulse response is

$$h[n] = \left\lceil \frac{1}{3} \right\rceil^n u[n] + \left\lceil \frac{1}{2} \right\rceil^n u[n-1].$$
 (08 Marks)

OR

10 a. Using power series expansion technique or long division method find the inverse z-transform of the following X(z).

i)
$$X(z) = \frac{z}{2z^2 - 3z + 1}$$
; ROC $|z| < \frac{1}{2}$

- ii) $X(z) = \frac{z}{2z^2 3z + 1}$; ROC |z| > 1. (08 Marks)
- b. Determine the z-transform of the following signal $x[n] = 2^n u[n]$.

 Also obtain ROC and locations of poles and zeroes of X(z).

 (06 Marks)
- c. Using z-transform find the convolution of the following two sequences

$$\begin{split} h[n] &= \left\{ \begin{matrix} 1 \\ \uparrow \end{matrix}, \ \frac{1}{2}, \ \frac{1}{4} \right\} \text{and} \\ x[n] &= \delta \left[n \right] + \delta \left[n-1 \right] + 4\delta \left(n-2 \right). \end{split} \tag{06 Marks} \end{split}$$

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